

ESERCIZI SULLE EQUAZIONI DI 2° GRADO A COEFFICIENTI IRRAZIONALI:
CORREZIONI

73)

$$x^2 + 4 = 3x\sqrt{2} \quad x^2 - 3x\sqrt{2} + 4 = 0$$

$$x_{1,2} = \frac{3\sqrt{2} \pm \sqrt{(3\sqrt{2})^2 - 16}}{2} = \frac{3\sqrt{2} \pm \sqrt{18-16}}{2} = \frac{3\sqrt{2} \pm \sqrt{2}}{2} = \begin{cases} \frac{2\sqrt{2}}{2} = \boxed{\sqrt{2}} \\ \frac{4\sqrt{2}}{2} = \boxed{2\sqrt{2}} \end{cases}$$

74)

$$2x(\sqrt{2} - x) = 1 \quad 2x\sqrt{2} - 2x^2 = 1 \quad -2x^2 + 2x\sqrt{2} - 1 = 0 \quad 2x^2 - 2x\sqrt{2} + 1 = 0$$

$$x_{1,2} = \frac{\sqrt{2} \pm \sqrt{2-2}}{2} = \frac{\sqrt{2} \pm 0}{2} = \boxed{\frac{\sqrt{2}}{2}}$$

75)

$$(x\sqrt{3}-1)(2x\sqrt{3}-1) = 0$$

Senza svolgere i calcoli,
dato che abbiamo già a primo membro una scomposizione in fattori
e il secondo membro è 0:

$$x\sqrt{3}-1=0, \quad x = \frac{1}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \boxed{\frac{\sqrt{3}}{3}}$$

$$2x\sqrt{3}-1=0, \quad x = \frac{1}{2\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}} = \boxed{\frac{\sqrt{3}}{6}}$$

76)

$$9x^2 + 2\sqrt{3} = 4$$

$$9x^2 = 4 - 2\sqrt{3}$$

$$x^2 = \frac{4 - 2\sqrt{3}}{9}$$

$$x = \pm \sqrt{\frac{4 - 2\sqrt{3}}{9}} = \pm \frac{\sqrt{4 - 2\sqrt{3}}}{3} = \pm \frac{\sqrt{(\sqrt{3}-1)^2}}{3} = \boxed{\pm \frac{\sqrt{3}-1}{3}}$$

78)

$$9x^2 + 2\sqrt{3} = 3$$

$$9x^2 = 3 - 2\sqrt{3}$$

$$x^2 = \frac{3 - 2\sqrt{3}}{9} \quad [\text{impossibile}],$$

perchè $3 - 2\sqrt{3} < 0$ quindi anche $\frac{3 - 2\sqrt{3}}{9} < 0$

81)

$$\begin{aligned}
 & (x+4) \cdot \frac{x-4}{x-1} - 2 \cdot \frac{x+2\sqrt{6}}{1-x} = 2 \\
 & \frac{x^2-16}{x-1} + \frac{2x+4\sqrt{6}}{x-1} = 2 \\
 & x^2-16 \cancel{+ 2x+4\sqrt{6}} = 2x-2 \quad (x \neq 1) \\
 & x^2 = 14-4\sqrt{6} \\
 & x = \pm \sqrt{14-4\sqrt{6}} = \pm \sqrt{(2\sqrt{3}-\sqrt{2})^2} = \boxed{\pm(2\sqrt{3}-\sqrt{2})}
 \end{aligned}$$

84)

$$\begin{aligned}
 & 2x^2 - 3x(1+\sqrt{2}) + \sqrt{2} = 0 \quad \boxed{a=2 \quad b=-3(1+\sqrt{2}) \quad c=\sqrt{2}} \\
 & x_{1,2} = \frac{3(1+\sqrt{2}) \pm \sqrt{9(1+\sqrt{2})^2 - 8\sqrt{2}}}{4} = \frac{3(1+\sqrt{2}) \pm \sqrt{9+18\sqrt{2}+18-8\sqrt{2}}}{4} = \\
 & = \frac{3(1+\sqrt{2}) \pm \sqrt{27+10\sqrt{2}}}{4} = \frac{3(1+\sqrt{2}) \pm \sqrt{(5+\sqrt{2})^2}}{4} = \frac{3(1+\sqrt{2}) \pm (5+\sqrt{2})}{4} = \\
 & = \begin{cases} \frac{3(1+\sqrt{2})-(5+\sqrt{2})}{4} = \frac{3+3\sqrt{2}-5-\sqrt{2}}{4} = \frac{2\sqrt{2}-2}{4} = \frac{\cancel{2}(\sqrt{2}-1)}{\cancel{4}^2} = \boxed{\frac{\sqrt{2}-1}{2}} \\ \frac{3(1+\sqrt{2})+(5+\sqrt{2})}{4} = \frac{3+3\sqrt{2}+5+\sqrt{2}}{4} = \frac{4\sqrt{2}+8}{4} = \frac{\cancel{4}(\sqrt{2}+2)}{\cancel{4}} = \boxed{\sqrt{2}+2} \end{cases}
 \end{aligned}$$

87)

$$\begin{aligned}
 & 3x+\sqrt{3}(3x-5)=x^2+8 \quad 3x+3x\sqrt{3}-5\sqrt{3}=x^2+8 \quad -x^2+3x+3x\sqrt{3}-5\sqrt{3}-8=0 \\
 & x^2-3x-3x\sqrt{3}+5\sqrt{3}+8=0 \quad x^2-3x(1+\sqrt{3})+(5\sqrt{3}+8)=0 \\
 & x_{1,2} = \frac{3(1+\sqrt{3}) \pm \sqrt{9(1+\sqrt{3})^2 - 4(5\sqrt{3}+8)}}{2} = \frac{3(1+\sqrt{3}) \pm \sqrt{9(1+2\sqrt{3}+3)-20\sqrt{3}-32}}{2} = \\
 & = \frac{3(1+\sqrt{3}) \pm \sqrt{4-2\sqrt{3}}}{2} = \frac{3(1+\sqrt{3}) \pm \sqrt{(\sqrt{3}-1)^2}}{2} = \frac{3+3\sqrt{3} \pm (\sqrt{3}-1)}{2} = \begin{cases} \frac{2\sqrt{3}+4}{2} = \boxed{\sqrt{3}+2} \\ \frac{4\sqrt{3}+2}{2} = \boxed{2\sqrt{3}+1} \end{cases}
 \end{aligned}$$

92)

$$\begin{aligned}
 & 3x^2\sqrt{2} + x(3x-1) = 2x \\
 & 3x^2\sqrt{2} + 3x^2 - x = 2x \\
 & \cancel{3}x^2\sqrt{2} + \cancel{3}x^2 - \cancel{3}x = 0 \\
 & x(x\sqrt{2} + x - 1) = 0 \\
 & x[x(\sqrt{2}+1)-1] = 0 \\
 & x = \boxed{0} \quad \vee \quad x(\sqrt{2}+1)-1 = 0; \\
 & x = \frac{1}{\sqrt{2}+1} \cdot \frac{\sqrt{2}-1}{\sqrt{2}-1} = \frac{\sqrt{2}-1}{1} = \boxed{\sqrt{2}-1}
 \end{aligned}$$